

# Thermoelectric Power Generator Design for Maximum Power: It's All About $ZT$

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There is a significant amount of literature that discusses thermoelectric power generator (TEG) design, but much of it overly simplifies the design space and therefore the results have limited use in designing real-life systems. This paper develops a more comprehensive model of the thermal and electrical interactions of a TEG in a system with known hot-side and cold-side thermal resistances and corresponding constant system temperature differential. Two design scenarios are investigated for common TEG system applications. In one method, the power from a TEG is maximized for a given electrical load, simulating a case where the TEG is electrically in series with a known load such as a fan. In the second design scenario, the power from a TEG is maximized for a given electrical load resistance ratio,  $n$  (the ratio between the external load resistance and the internal TEG resistance), simulating an application where the TEG is electrically in series with a load-matching converter. An interesting conclusion from this work is that, in the first design scenario, the electrical load resistance ratio,  $n$ , that maximizes TEG power occurs at  $\sqrt{1 + ZT}$  (where  $ZT$  is the thermoelectric figure of merit) instead of 1 as reported previously in literature. Equally interesting is that, if you define an analogous thermal resistance ratio,  $m'$  (representing the ratio between the TEG thermal resistance at open-circuit conditions and the system thermal resistance), the maximum power in both design scenarios occurs at  $\sqrt{1 + ZT}$  instead of the commonly cited value of 1. Furthermore, results are presented for real-life designs that incorporate electrical and thermal losses common to realistic TEG systems such as electrical contact resistance and thermal bypass around the TEG due to sealing.

**Key words:** Thermoelectric device, maximum power, optimal design

## INTRODUCTION

Designing an optimal thermoelectric generator (TEG) in a system with thermal resistance (heat sinks) on either side of the TEG is common in many applications. In some of these applications, the TEG is wired in series with a known fixed electrical load such as a fan, whereas in other applications, the TEG is wired in series with an electrical load that can maintain the ratio between the load and internal resistance of the TEG, such as a load-matching converter. In both cases, the design of the TEG [the

geometry of the individual thermoelectric (TE) elements and the number of these elements] can be found by optimizing the TEG power.

A typical TEG system is shown in Fig. 1 and includes heat sinks on the hot side and cold side of the TEG with defined thermal resistance of HSR and CSR, respectively. The heat source is at  $T_{\text{Source}}$  and the heat sink is at  $T_{\text{Amb}}$  temperatures. Heat flows from  $T_{\text{Source}}$  through the heat sink and TEG to  $T_{\text{Amb}}$ . If there is a thermal bypass around the TEG, then heat also flows in parallel with  $C_{\text{Loss}}$ . The temperatures across the TEG are  $T_{\text{H}}$  and  $T_{\text{C}}$ , respectively. The TEG is wired electrically in series with an electric load  $R_{\text{Load}}$ . The TEG is made of  $N$  number of couples with length-to-area ratio of  $\lambda$  (Table I).

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